

# Tamper and Leakage Resilience in the Split State Model

Feng-Hao Liu

Anna Lysyanskaya

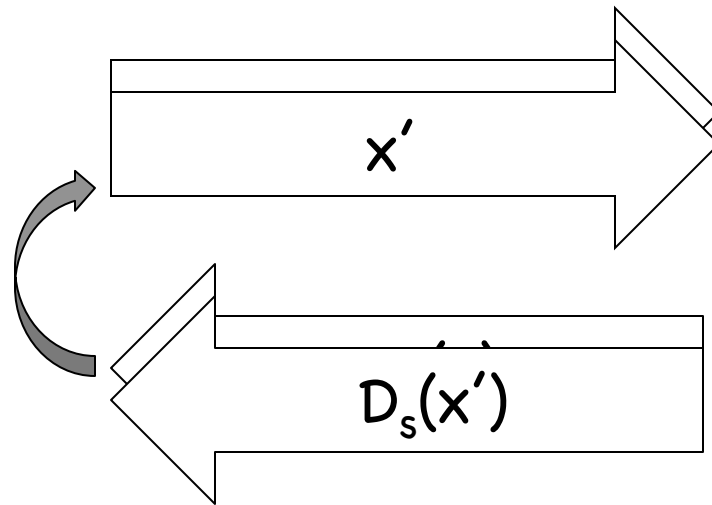
Brown University



# I/O Access to a Device



User

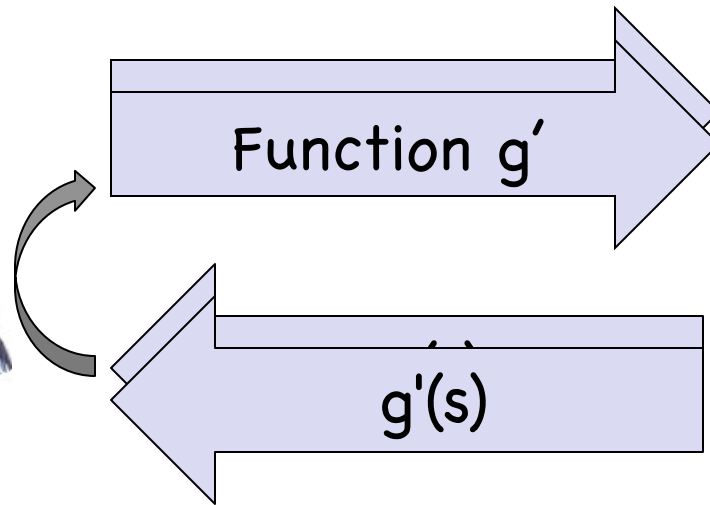


Device for  $D_s(\bullet)$

# Leakage/Side Channel Attack [Kocher96,HSHCP+08...]



Adversary

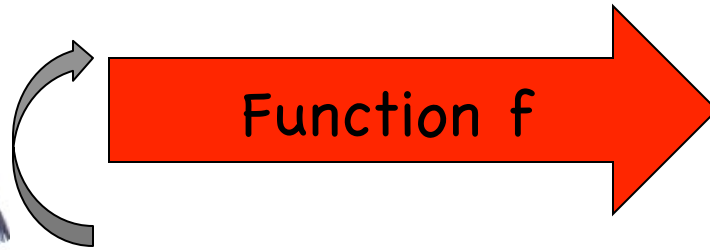


Device for  $D_s(\bullet)$

# Tampering Attack [BS97,AARR02...]

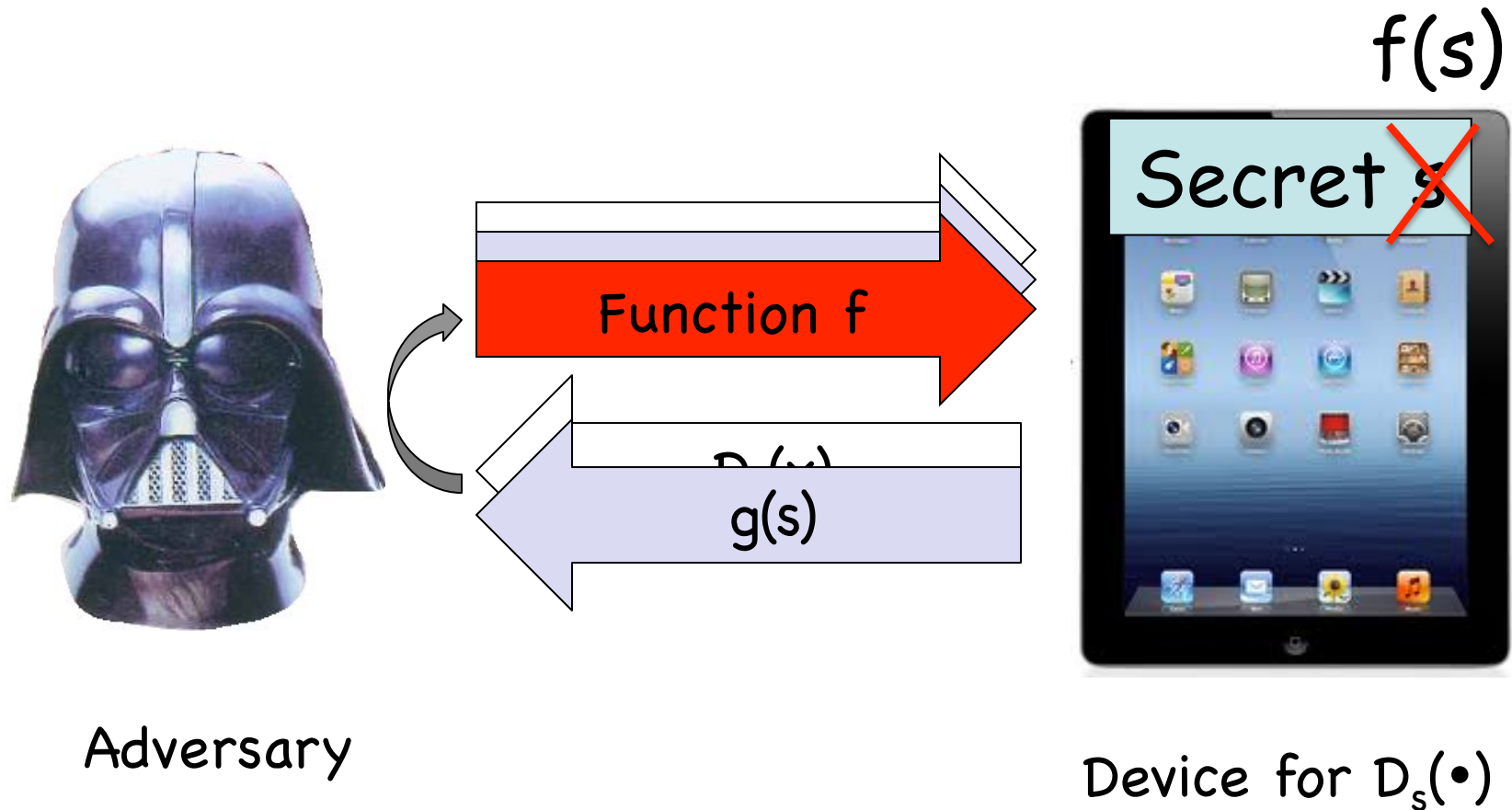


Adversary



Device for  $D_s(\bullet)$

# Continuous L+T Attack [LL10,KKS11]



Remark: in this model, computations (updates) happen between the attacks, unlike the model of [MR04]

# Previous Work

- Tampering only [GLMMR04,DPW10,CKM11]
- Leakage only [AGV09,NS09,KV09,  
DHLW10,BKKV10,DLWW11...]
- Combined attack:
  - Negative results: [LL10] how to leak from the future if have no randomness, even in very restricted attack models
  - Positive results: [KKS11] encryption and signatures if have fresh randomness on update

Where do you get fresh  
randomness while under  
attack??

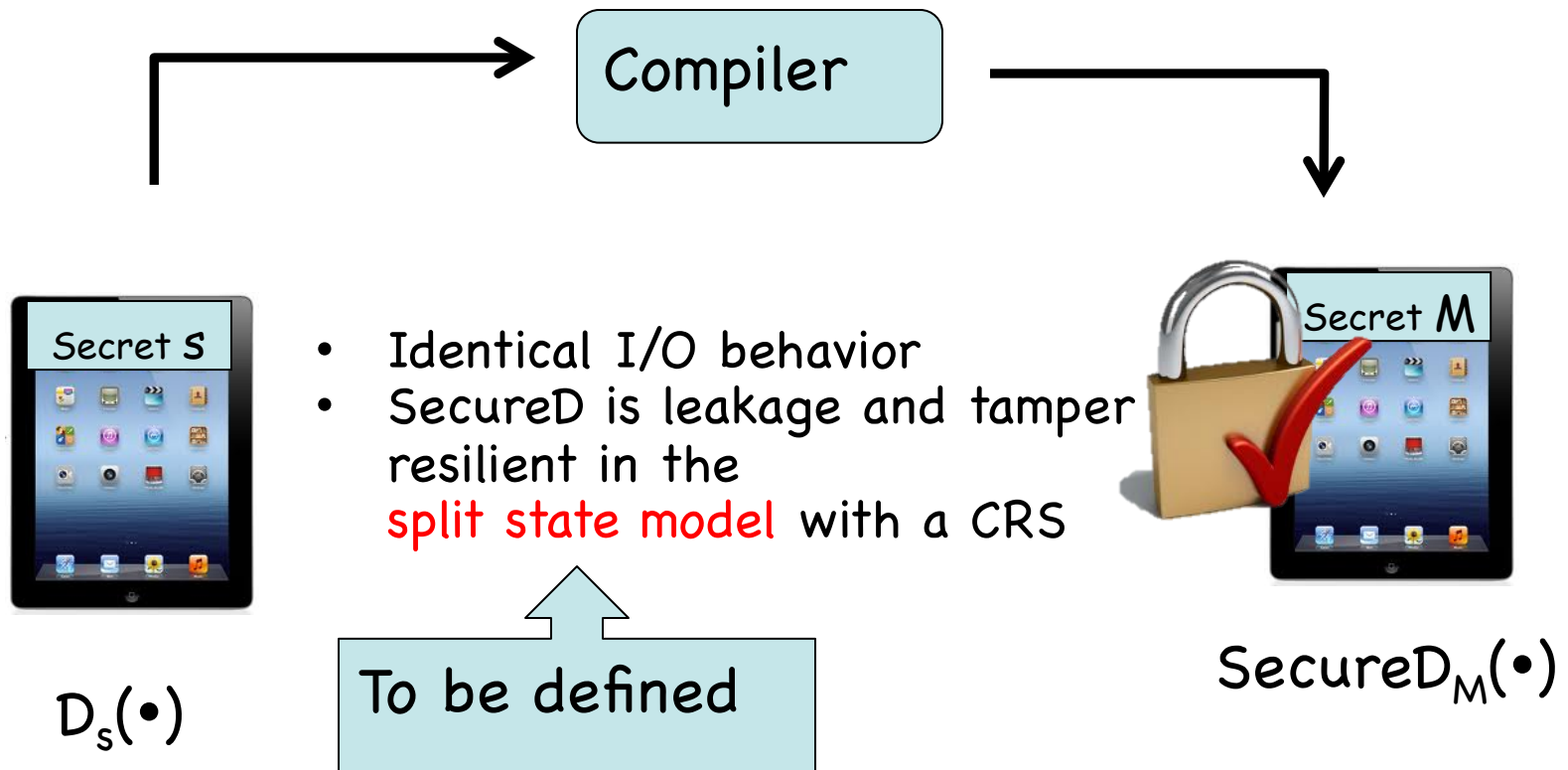
# Our Goal

- An architecture that can tolerate leakage and tampering attacks at the same time...
  - without assuming an on-device source of randomness
  - under a reasonable restriction on the adversary's leakage and tampering power



# Our Main Result

- A compiler: given  $D$ , produces  $\text{Secure}D$



# The Split State Model

[DPW10,DLWW11,HL11...]

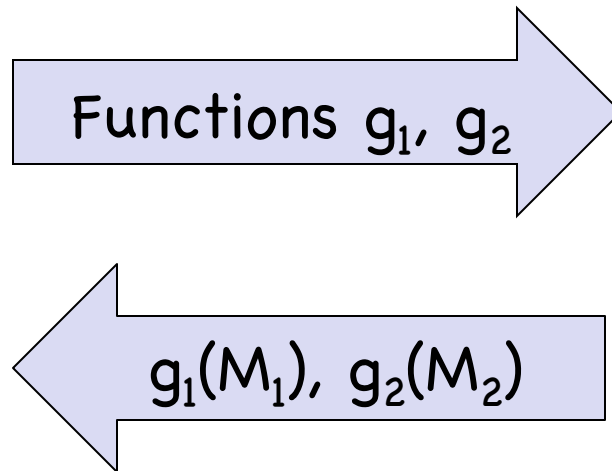


The two parts are attacked separately

# Split State Model: Leakage



Adversary



Device for  $D_{M_1, M_2}(\bullet)$

# Split State Model: Tampering



Adversary

Functions  $f_1, f_2$



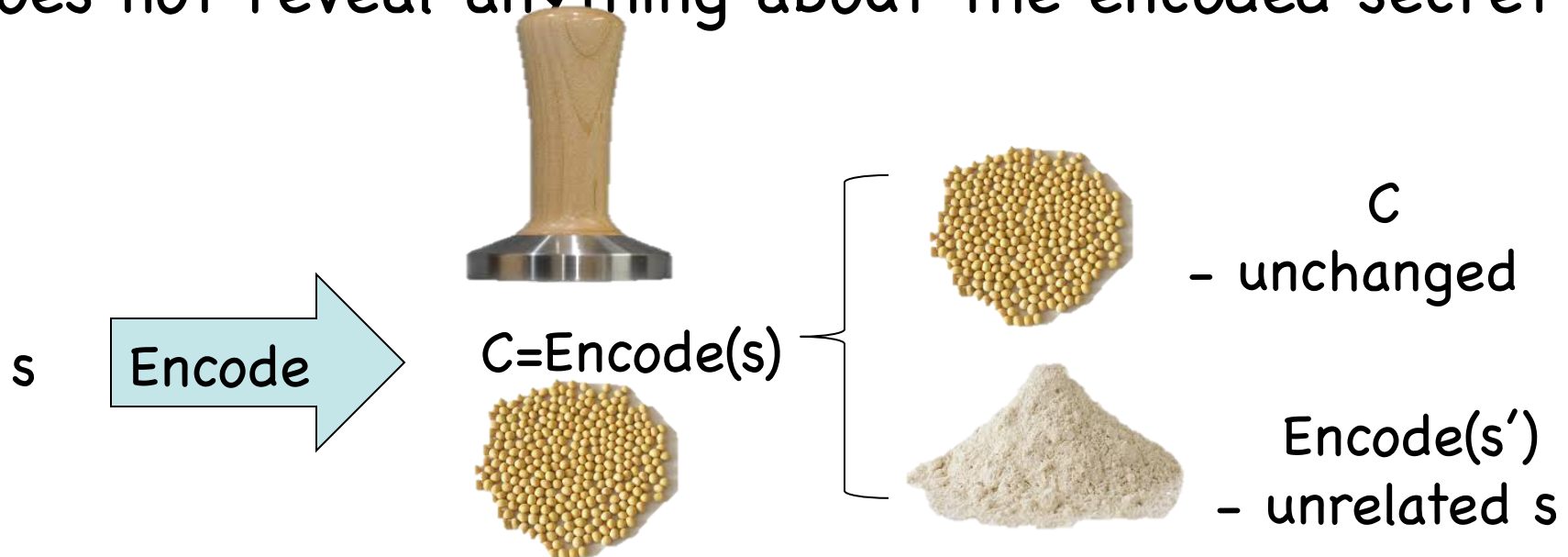
$f_1(M_1)$

$f_2(M_2)$

Device for  $D_{M_1, M_2}(\bullet)$

# Towards Tamper-Resilience: Non-Malleable Code [DPW10]

- Encode  $s$  into  $C = (M_1, M_2)$  s.t. tampering is useless!
- Non-malleable code [DPW10]: “mauling” the code does not reveal anything about the encoded secret



# Non-Malleable Code

- Formally: for all  $f$  in  $F$ , all  $s, s'$ ,

$$\text{Tamper}_{\text{ppt}}(f,s) \approx \text{Tamper}(f,s')$$

$$\text{Tamper}(f,s) = \begin{cases} \text{"same" if } f(c) = c, \text{ where } c \leftarrow \text{Encode}(s) \\ \text{Decode}(f(c)) \text{ otherwise} \end{cases}$$

The diagram illustrates the definition of the Tamper function. On the left, the expression  $\text{Tamper}(f,s)$  is shown with a light blue box labeled 'CRS' below it, and an upward-pointing arrow from the box to the 's' in the function. A large right-facing curly bracket groups the two cases of the function's definition. The first case is "same" if  $f(c) = c$ , where  $c \leftarrow \text{Encode}(s)$ . Below this case is another light blue box labeled 'CRS' with an upward-pointing arrow to the 's' in  $\text{Encode}(s)$ . The second case is  $\text{Decode}(f(c))$  otherwise. Below this case is a third light blue box labeled 'CRS' with an upward-pointing arrow to the 'c' in  $f(c)$ .

Impossible in general, but

- [DPW10] construct them in SS RO model, unbounded functions
- We construct them in SS CRS model, poly-sized functions

# NM Code Protects from Tampering Attack [DPW10]

Adversary's view  
in real attack:



Function  $f$

~~$C = \text{Encode}(s)$~~

$\text{Decode}(f(C))$

Adversary's view  
in a simulation:



Function  $f$

~~$C' = \text{Enc}(000)$~~

$\text{Decode}(f(C'))$

# NM Code in the SS Model: Our Construction

$$\text{Encode}(s) = \boxed{M_1 = sk} \quad \boxed{M_2 = (pk, C = \text{Enc}_{pk}(s), \pi)}$$

- the encryption scheme is leakage-resilient
- unique  $pk$  for each  $sk$ , unique  $sk$  for each  $pk$  (\*)
- $\pi$  is a non-malleable (robust) NIZK PoK of  $sk$  and the decryption of  $C$

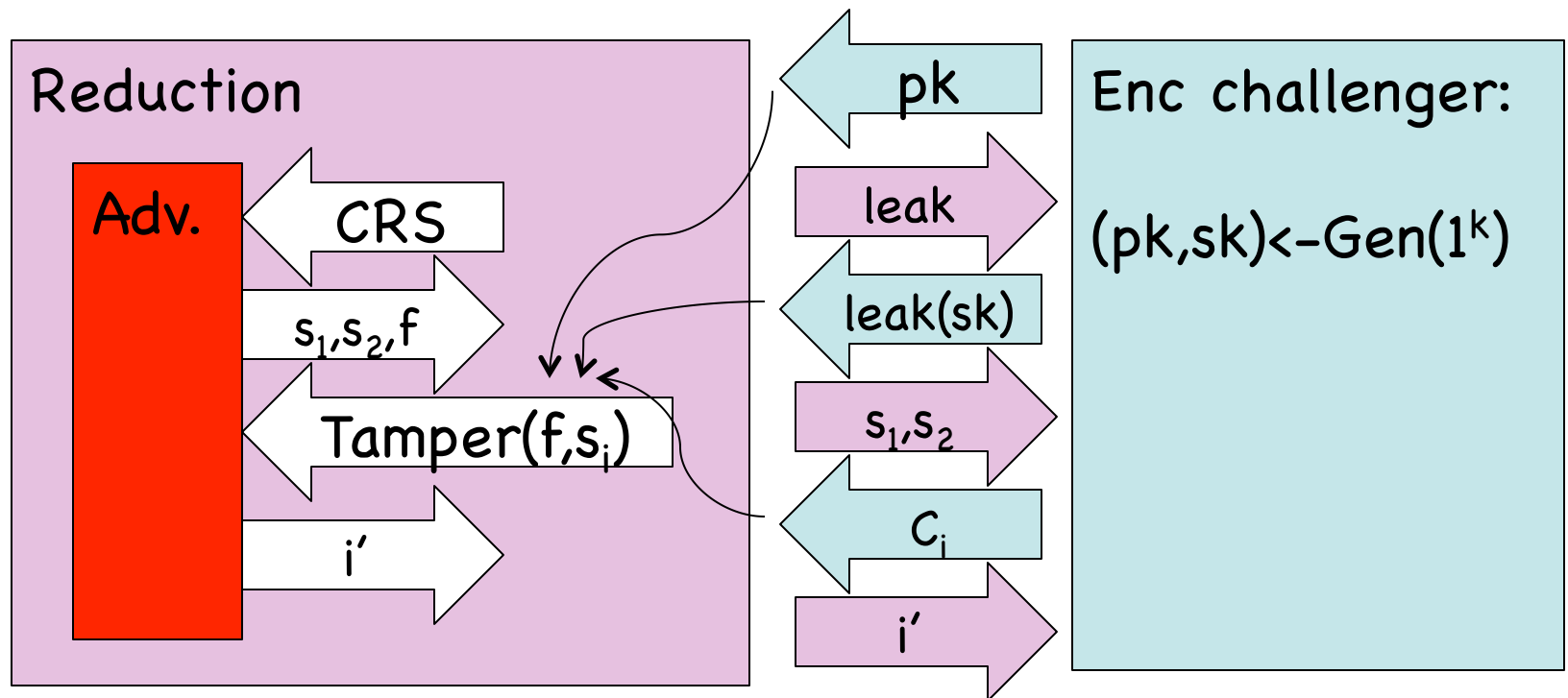
Robust NIZK PoK [DDOPS01]: even with access to a ZK simulator, Adv can only produce proofs whose witnesses can be extracted (similar to UC NIZK)



# Proof of Security of Our NM Code

Suppose this is not a NM code. Then there exist  $s_1, s_2, f=(f_1, f_2)$  such that  $\text{Tamper}(f, s_1)$  can be distinguished from  $\text{Tamper}(f, s_2)$ .

Use that to break encryption:



# Proof

Suppose this  
such that Tam

Tamper(f,s) =

"same" if  $f(c) = c$ , where  $c \leftarrow \text{Encode}(s)$

Decode(f(c)) otherwise

Use the

(Hopefully)  
don't need

h:  $(pk, C_1 = \text{Enc}_{pk}(s_1))$  from  $(pk, C_2 = \text{Enc}_{pk}(s_2))$ :

Reduction computes Tamper(f,s) as follows:

$M_1 = sk$ ,  $M_2 = (pk, C_i, \pi)$

Use ZK  
simulator

recall  $f = (f_1, f_2)$

$M_2' = (pk', C', \pi') = f_2(M_2)$ ;

if  $M_2' \neq M_2$  then:

if  $\pi'$  invalid, output NULL

else extract  $(s', sk')$  from  $\pi'$

Robust  
NIZK Pok

if  $sk' = f_1(M_1)$  output  $s'$ , else NULL

else if  $M_2' = M_2$  : if  $f_1(M_1) = sk$  output

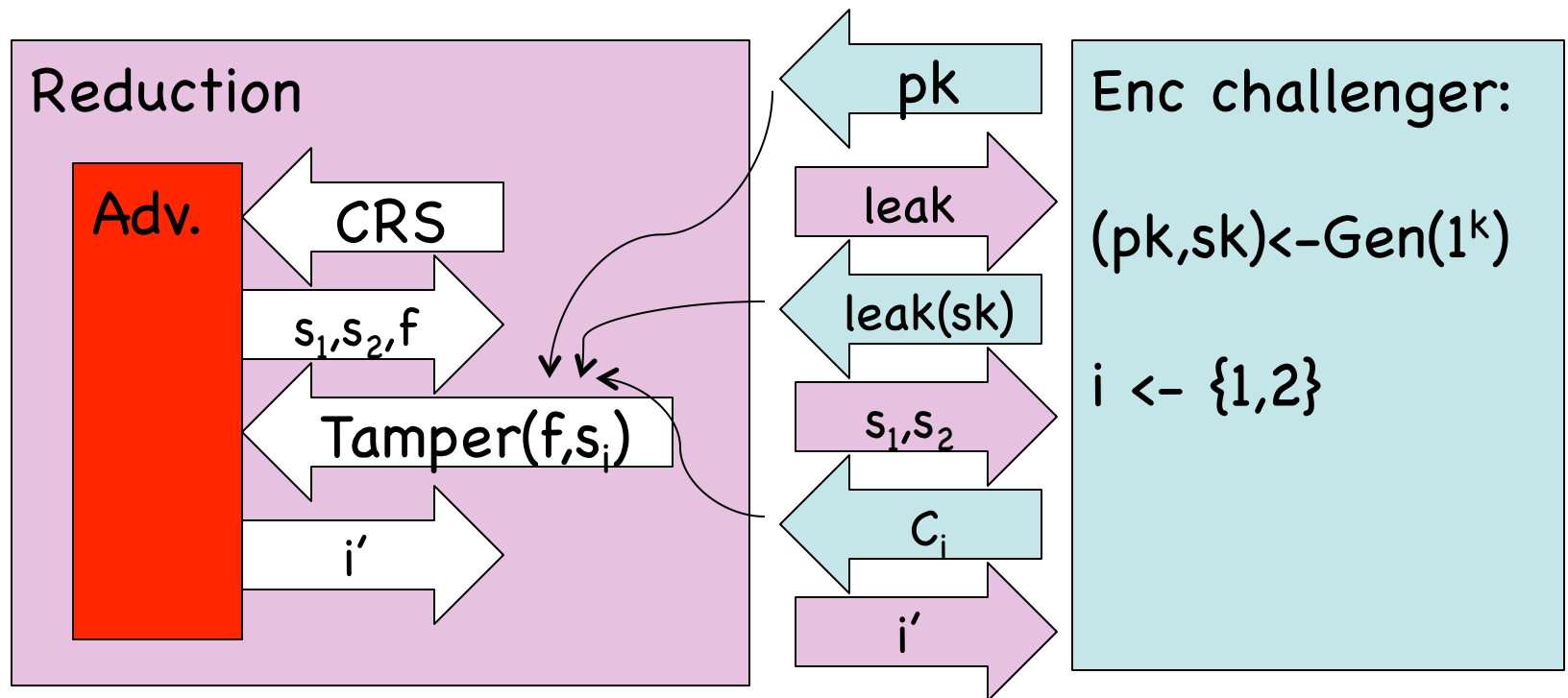
Use leakage  
query here

NULL

# Proof of Security of Our NM Code

Suppose this is not a NM code. Then there exist  $s_1, s_2, f=(f_1, f_2)$  such that  $\text{Tamper}(f, s_1)$  can be distinguished from  $\text{Tamper}(f, s_2)$ .

Use that to break encryption:

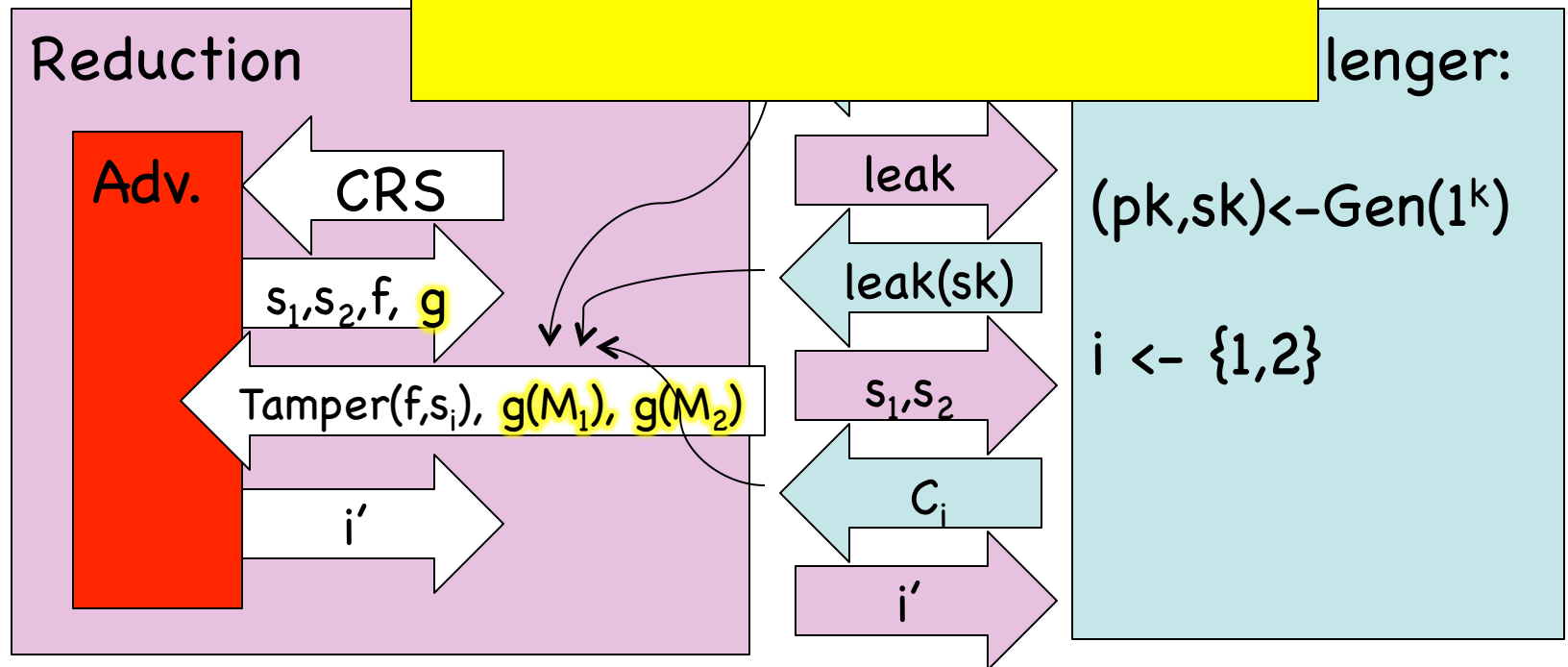


# Proof of Security of Our NM Code

Suppose this is not a NM code. Then there exist  $s_1, s_2, f=(f_1, f_2)$  such that  $\text{Tamper}(f, s_1)$  can be distinguished from  $\text{Tamper}(f, s_2)$ .

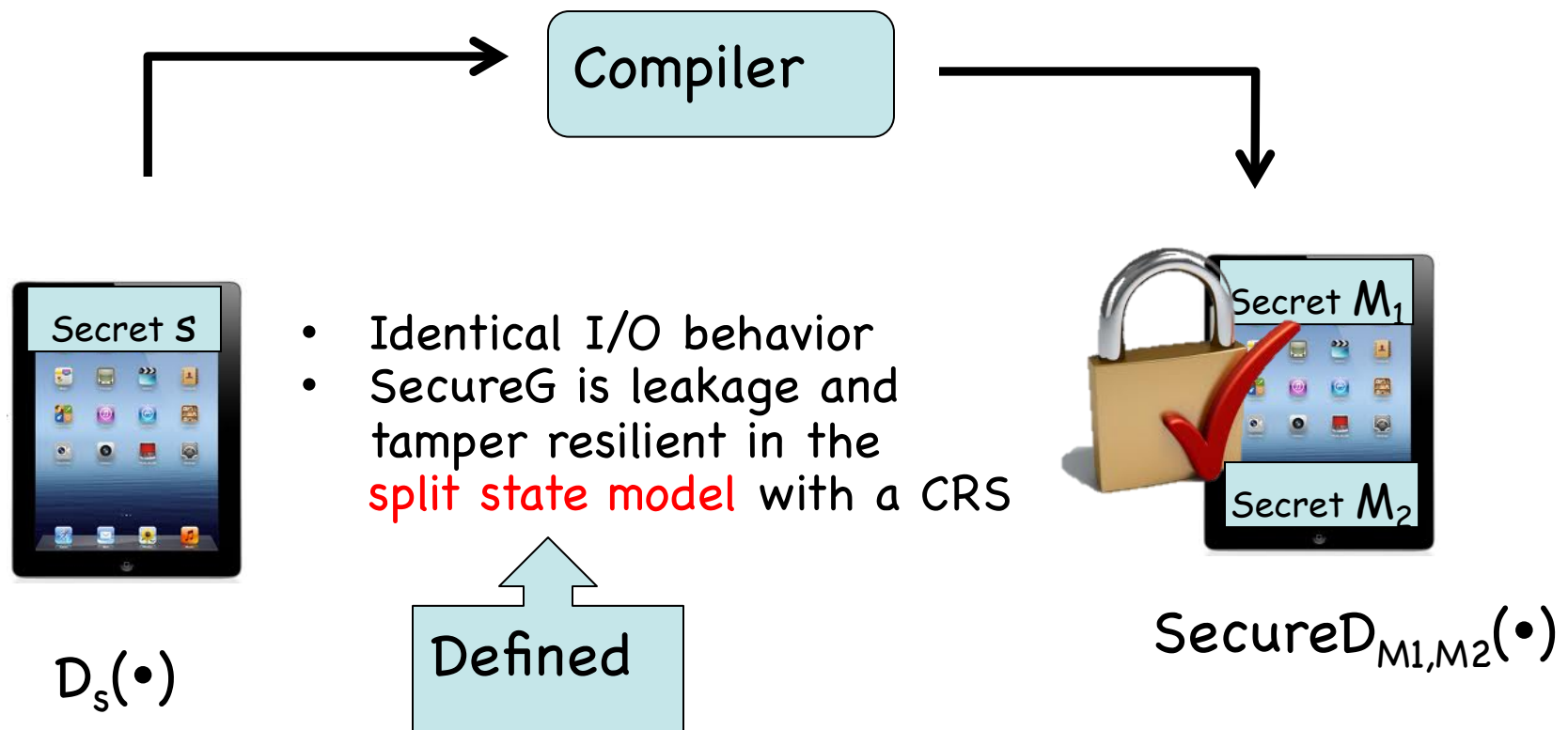
Use that to break e

Bonus!! Our NM code is also leakage-resilient in SS model!



# LR NM Codes $\Rightarrow$ L+T Resilience

- A compiler: given  $D$ , produces  $\text{Secure}D$



# Our L+T Resilient Compiler: Construction 1 (Randomized)



Compiler

$(M_1, M_2) = \text{Encode}(s)$  using  
the LR NM code



$D_s(\bullet)$

$\text{SecureD}_{M_1, M_2}(x)$ :

$s = \text{Decode}(M_1, M_2)$

refresh:  $(M_1, M_2) \leftarrow \text{Encode}(s)$

output  $D_s(x)$

Here use  
randomness

# Our L+T Resilient Compiler: Construction 2 (Deterministic)



Compiler

$(M_1, M_2) = \text{Encode}(s, \text{seed})$  using  
the LR NM code



$D_s(\bullet)$

$\text{Secured}_{M_1, M_2}(x):$

$(s, \text{seed}) = \text{Decode}(M_1, M_2)$

$\text{rand}, \text{seed}' = \text{PRG}(\text{seed})$

refresh:  $(M_1, M_2) = \text{Encode}(s, \text{seed}')$  using  $\text{rand}$  as coins

output  $D_s(x)$

# CONCLUSION

Traded off perfect randomness for SS model:

- got L+T resilience for EVERY functionality
- after-the-fact leakage and tampering resilience (solved open problems of [HL11])
- achieved simulation based security

Of independent interest: new NM code  
(solved open problems of [DPW10])